General Certificate of Education (A-level) June 2012

## Mathematics

MPC2

## (Specification 6360)

Pure Core 2

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all examiners participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the students' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for standardisation each examiner analyses a number of students' scripts: alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, examiners encounter unusual answers which have not been raised they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of students' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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## Key to mark scheme abbreviations

| M | mark is for method |
| :--- | :--- |
| m or dM | mark is dependent on one or more M marks and is for method |
| A | mark is dependent on M or m marks and is for accuracy |
| B | mark is independent of M or m marks and is for method and accuracy |
| E | mark is for explanation |
| Jor ft or F | follow through from previous incorrect result |
| CAO | correct answer only |
| CSO | correct solution only |
| AWFW | anything which falls within |
| AWRT | anything which rounds to |
| ACF | any correct form |
| AG | answer given |
| SC | special case |
| OE | or equivalent |
| A2,1 | 2 or 1 (or 0) accuracy marks |
| $-x$ EE | deduct $x$ marks for each error |
| NMS | no method shown |
| PI | possibly implied |
| SCA | substantially correct approach |
| c | candidate |
| sf | significant figure(s) |
| dp | decimal place(s) |

## No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award full marks. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn no marks.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.
Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns full marks, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains no marks.

Otherwise we require evidence of a correct method for any marks to be awarded.

## General Certificate of Education

 MPC2 June 2012\begin{tabular}{|c|c|c|c|c|}
\hline Q \& Solution \& Marks \& Total \& Comments \\
\hline \begin{tabular}{l}
1(a) \\
(b) \\
(c)
\end{tabular} \& \[
\begin{aligned}
\& (\text { common difference })=9 \\
\& (100 \text { th term })=23+(100-1) d \\
\& =914 \\
\& (\text { Sum of series })=\frac{280}{2}(23+2534) \\
\& \left\{\text { or } \frac{280}{2}[2 \times 23+(280-1)(9)]\right\} \\
\& =357980
\end{aligned}
\] \& \begin{tabular}{l}
B1 \\
M1 \\
A1 \\
M1 \\
A1
\end{tabular} \& 1
2
2

2 \& | 9 |
| :--- |
| $23+(100-1) d$ or better seen (or used with $d=9$ or with $d=$ c's answer (a)) 914 NMS mark as B2 or B0 |
| Substitution of $n=280, l=2534$, $a=23$ (or c's value of $a$ used in (b)), $d=9\left(\right.$ or c's answer to (a)) into $\frac{n}{2}(a+l)$ PI or $\frac{n}{2}[2 a+(n-1) d]$ PI |
| 357980 NMS mark as B2 or B0 | <br>

\hline \& Total \& \& 5 \& <br>

\hline | 2(a) |
| :--- |
| (b) |
| (c) | \& \[

$$
\begin{aligned}
& \text { (Area) }=\frac{1}{2}(26)(31.5) \sin \theta \\
& \frac{1}{2}(26)(31.5) \times \frac{5}{13}=157.5\left(\mathrm{~cm}^{2}\right) \\
& (\cos \theta=) \frac{12}{13} \\
& \left\{A C^{2}=\right\} \\
& 31.5^{2}+26^{2}-2 \times 31.5 \times 26 \times \cos (\theta) \\
& =992.25+676-1512 \\
& =1668.25-1512=156.25 \\
& A C=\sqrt{156.25}=12.5(\mathrm{~cm}) \\
& (\text { Alternative }) \\
& \left\{A C^{2}=\right\}(26 \sin \theta)^{2}+(31.5-26 \cos \theta)^{2} \\
& =10^{2}+7.5^{2} \\
& A C=\sqrt{156.25}=12.5(\mathrm{~cm})
\end{aligned}
$$

\] \& | M1 |
| :--- |
| A1 |
| B1 |
| M1 |
| m1 |
| A1 |
| (M1) |
| (m1) |
| (A1) | \& | 2 |
| :--- |
| 1 |
| 3 |
| (3) | \& | $\frac{1}{2}(26)(31.5) \sin (\theta)$ stated or used OE eg $\frac{315}{2}$ |
| :--- |
| Condone AWRT 157.50 |
| NMS: 157.5 or AWRT 157.50 scores B2 |
| $\frac{12}{13}$ OE exact fraction |
| RHS of cosine rule |
| Correct order of evaluation. Do not award if evaluation leads to or would lead to RHS value being outside interval 120 to 195 |
| 12.5 OE with no sight of premature approximation clearly used | <br>

\hline \& Total \& \& 6 \& <br>
\hline
\end{tabular}

\begin{tabular}{|c|c|c|c|c|}
\hline Q \& Solution \& Marks \& Total \& Comments \\
\hline 3(a) \& \[
\ldots \ldots=\left(x^{\frac{3}{2}}\right)^{2}-2 x^{\frac{3}{2}}+1=x^{3}-2 x^{\frac{3}{2}}+1
\] \& B2,1,0 \& 2 \& B2 for \(x^{3}-2 x^{\frac{3}{2}}+1\) or \(x^{3}-2 x \sqrt{x}+1\) (B1 fully correct unsimplified expression. seen eg \(\left(x^{\frac{3}{2}}\right)^{2}-x^{\frac{3}{2}}-x^{\frac{3}{2}}+1\) or B1 for either \(x^{3}-2 x^{\frac{3}{2}} \ldots\) OE seen or \(x^{3}+2 x^{\frac{3}{2}}+1\) OE seen or B1 for \(-x^{3}+2 x^{\frac{3}{2}}-1\) OE seen) \\
\hline (b) \& \[
\int\left(x^{\frac{3}{2}}-1\right)^{2} \mathrm{~d} x=\frac{x^{4}}{4}-\frac{2 x^{\frac{5}{2}}}{2.5}+x(+c)
\] \& B1F \& \& Ft on correct integration of all non \(x^{\frac{3}{2}}\) terms (at least two) in c's expression. in (a) \\
\hline \& \[
\left\{=0.25 x^{4}-0.8 x^{2.5}+x(+c)\right\}
\] \& M1
A1F \& 3 \& \begin{tabular}{l}
Integration of a \(k x^{\frac{3}{2}}\) as \(\lambda x^{\frac{5}{2}}\) (ie power correct) \\
Correct integration of c 's \(x^{\frac{3}{2}}\) term(s) ACF
\end{tabular} \\
\hline (c) \& \[
\begin{aligned}
\& \int_{1}^{4}\left(x^{\frac{3}{2}}-1\right)^{2} \mathrm{~d} x \\
\& =\left(\frac{4^{4}}{4}-\frac{2\left(4^{\frac{5}{2}}\right)}{2.5}+4\right)-\left(\frac{1}{4}-\frac{2}{2.5}+1\right) \\
\& \left\{=\frac{212}{5}-\frac{9}{20}=42.4-0.45\right\}=41.95
\end{aligned}
\] \& M1

A1 \& 2 \& | $F(4)-F(1)$ attempted following integration. If $\mathrm{F}(x)$ incorrect, ft c 's answer to (b) provided integration attempted |
| :--- |
| 41.95 OE eg 839/20 |
| Since 'Hence' NMS scores $0 / 2$ | <br>

\hline \& Total \& \& 7 \& <br>
\hline
\end{tabular}




| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 6(a)(i) | $($ When $x=2) \frac{\mathrm{d} y}{\mathrm{~d} x}=12-1-11=0$ | B1 | 1 | AG Must see intermediate evaluations |
| (ii) | $\frac{4}{x^{2}}=4 x^{-2} \quad\left\{\text { so } \frac{\mathrm{d} y}{\mathrm{~d} x}=3 x^{2}-4 x^{-2}-11\right\}$ | B1 |  | $\frac{4}{x^{2}}=4 x^{-2}$, seen in (a)(ii) or earlier. PI by $\pm 8 x^{-3}$ term in answer |
|  | $\frac{\mathrm{d}^{2} y}{\mathrm{~d} x^{2}}=6 x+8 x^{-3}$ | M1 A1 |  | Correct powers of $x$ correctly obtained from differentiating the first two terms $6 x+8 x^{-3} \mathrm{ACF}$ |
|  | When $x=2, \frac{\mathrm{~d}^{2} y}{\mathrm{~d} x^{2}}=12+8 / 8=13$ | A1 | 4 |  |
| (iii) | Since $\frac{\mathrm{d}^{2} y}{\mathrm{~d} x^{2}}>0, P$ is a minimum point. | E1F | 1 | Ft on c's value of $y^{\prime \prime}(2)$ in (a)(ii) but must see reference to sign of $y^{\prime \prime}(2)$ either explicitly or as inequality, as well as the correct ft conclusion |
| (b) | $\int\left(3 x^{2}-\frac{4}{x^{2}}-11\right) \mathrm{d} x=x^{3}+4 x^{-1}-11 x(+c)$ | M1 |  | Attempt to integrate $\frac{\mathrm{d} y}{\mathrm{~d} x}$ with at least two |
|  | $(y=) x^{3}+4 x^{-1}-11 x(+c)$ | A1 |  | For $x^{3}+4 x^{-1}-11 x$ OE even unsimplified Substituting. $x=2, y=1$ into $y=\mathrm{F}(x)+$ |
|  | When $x=2, y=1 \Rightarrow 1=8+2-22+c$ | M1 |  | integration, where $\mathrm{F}(x)$ follows attempted integration of expression for $\frac{\mathrm{d} y}{\mathrm{~d} x}$ |
|  | $y=x^{3}+4 x^{-1}-11 x+13$ | A1 | 4 | ACF |
|  | Total |  | 10 |  |



| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
|  |  | B1 |  | Correct shape, curve in $1^{\text {st }}$ two quadrants only, crossing positive $y$-axis once and asymptotic to negative $x$-axis. |
|  |  | B1 | 2 | Coordinates $(0,1)$. Accept $y$-intercept indicated as 1 on diagram or stated as 'intercept $=1$ ' B0 if graph clearly drawn crossing axes at more than one point |
| (b)(i) | $y^{2}-12=y \text { OE; } \quad 7^{2 x}-12=7^{x} \text { OE }$ $(y-4)(y+3)(=0) ;\left(7^{x}-4\right)\left(7^{x}+3\right)(=0)$ | M1 A1 |  | Eliminates either $x$ or $y$ correctly Correct factors or $y=\frac{1 \pm \sqrt{49}}{2}$ or better or $7^{x}=\frac{1 \pm \sqrt{49}}{2}$ or better |
|  | Since $y\left(=7^{x}\right)>0,\left[y\left(=7^{x}\right) \neq-3\right]$ (there is exactly one point of intersection) | E1 |  | Clear indication that c's negative solution(s) has/have been considered and rejected |
|  | $y$-coordinate is 4 | B1 | 4 |  |
| (ii) | $7^{x}=4 \text { so } x \log 7=\log 4\left[\text { or } x=\log _{7} 4\right]$ | M1 |  | OE ft on $7^{x}=k$, where $k$ is positive, to either $x \log 7=\log k$ or $x=\log _{7} k$ |
|  | $x=0.712(414 \ldots)=0.712$ to 3 SF | A1 | 2 | Condone > three significant figures. If use of logarithms not explicitly seen then score $0 / 2$ |




[^0]:    Further copies of this Mark Scheme are available from: aqa.org.uk

